$\begin{array}{c} \textbf{Interlayer binding energy of graphite} - \textbf{A direct experimental} \\ \textbf{determination} \end{array}$

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Abstract

Despite interlayer binding energy is one of the most important material properties for graphite, there is still lacking report on its direct experimental determination. In this paper, we present a novel experimental method to directly measure the interlayer binding energy of highly oriented pyrolytic graphite (HOPG). The obtained values of the binding energy are $0.27(\pm 0.02) J/m^2$, which can serve as a benchmark for other theoretical and experimental works.

Since the successful fabrication of monolayer graphene from highly oriented pyrolytic graphite (HOPG) in 2004 [1], great interests have been attracted by this perfect two-dimensional crystal made of carbon atoms. The superior electronic, thermal, and mechanical properties, and the large specific surface area make it a promising component in next generation of electronic devices, energy storage and conversion devices, water treatment application, and the smart (bio) materials [2–5]. Its inherent single layer structure determines that the application of graphene, to a large extent, rely on the detailed understanding and control of it interacts with its surroundings [6]. However, the nature and strength of interlayer binding in graphitic materials are poorly understood, despite that the binding strength in graphite/graphene is relevant to many key applications, such as graphene electronic devices fabricated on various substrates, graphite intercalation compounds in Li battery, carbon based system for hydrogen storage, and graphene based supercapacitors.

Experimentally, there is still lacking report on direct measurements of graphite interlayer binding energy (BE) and exfoliation energy (EE, the energy required to remove one graphene layer from a single-crystalline graphite) [7]. Although there are few reported values obtained indirectly, those values are quite discrepant. Based on the heat of wetting data, Girifalco et al. [8] obtained the EE value as 43 ± 5 meV/atom (or 0.26 ± 0.03 J/m²). By assuming the simple Lennard-Jones potential, they further estimated the BE to be about 18% larger than the EE, while the exact difference remains unknown. Benedict et al. [9] extrapolated the BE as 35^{+15}_{-10} meV/atom (or $0.21^{+0.09}_{-0.06}$ J/m²) from the measurement on the collapsed carbon nanotubes. More recently, Zacharia et al. [10] performed desorption experiments of aromatic molecules from a graphite surface and obtained the approximate graphite EE = 52 ± 5 meV/atom (or 0.32 ± 0.03 J/m²), which yields an estimate of the BE ~ 0.37 J/m².

Theoretically, modeling BE as well as EE for graphite is still a question mark due to the weak interlayer binding involving van der Waals interaction, which remains a notorious difficult to describe within the standard density functional theory (DFT) [7, 11]. The standard approximations used in DFT, such as local density approximation (LDA) and generalized gradient approximation (GGA), cannot accurately describe the long distance interaction such as van der Waals interactions. LDA calculations lead to good interlayer distance (e.g., 0.33nm) but binding energy is predicted as low as 24meV/atom (or 0.15 J/m²) [12]. An alternative is the van der Waals density functional method, which is developed to account the long-range part of the interactions by using an explicit nonlocal functional of den-

sity. However, the predicted interlayer distance is substantially higher than experimental value (e.g., 0.36, 0.376, vs. 0.334nm), the elastic modulus C_{33} is significantly lower (e.g., ~ 13 , 27 vs. 36GPa), and the binding energy is very scattered (e.g., 24meV/atom (or 0.15 J/m²), 45.5 meV/atom (or 0.28 J/m²), and 50 meV/atom (or 0.30 J/m²)) [12–14]. Until recently, two comprehensive first-principles calculations have been carried out. Spanu *et al.* [7] has employed the quantum Monte Carlo method to obtain the binding energy about 56meV/atom (or 0.34 J/m²), and Lebegue *et al.* [11] has used the adiabatic-connection fluctuation-dissipation theorem in the direct random approximation to obtain the binding energy as 48meV/atom (or 0.29 J/m²).

The above brief review shows a clear need of directly experimental determination of the BE for graphite. In this paper, we introduce a novel method to directly measure BE, which is motivated by our recent discovery of self-retraction motion phenomenon of micrometer graphite/SiO₂ flakes on graphite islands [15]. The idea is to assemble a thin graphite flake to span over a graphite step. As illustrated in Fig.1(a), the considered graphite flake consists of multilayered graphenes assembled in AB-stack, and the graphite step is single-crystalline with atomically smooth graphene top surfaces. The key of this experimental technique is to make the contact areas (C-D and E-F indicated in Fig. 1(a)) between the flake and the step in the AB-stack assembling. In our experiments, each graphite flake was coated on its top surface with a SiO_2 thin film. The deformation energy U of the above of graphite/ SiO_2 flake and graphite step can be modeled as a function of the step height Δ , the span length L, the thicknesses h_s and h_g of the SiO₂ film and the graphite flake, and the material elastic constants. Since a virtual increment δL of length L leads to the increase of the graphite surface area $2b \times \delta L$ and, consequently, the increment of the total surface energy $2\gamma b \times \delta L$, where b denotes the flake width and γ is the graphite basal plane surface energy, we obtain the equilibrium equation of the above system in the following form:

$$2\gamma = -\frac{1}{b}\frac{\partial U}{\partial L}.\tag{1}$$

Using the above-proposed method, we measured the interlayer binding energy, namely 2γ , of HOPG to be $0.27\pm0.02~\mathrm{J/m^2}$ (or $44\pm3~\mathrm{meV/atom}$). The details of our experiments are reported below.

The HOPG samples were purchased from Veeco (ZYH grade). As illustrated in Fig. 2(a), graphite islands were fabricated by using the same technique as that reported in Ref.

[16]. After mechanical exfoliation, a clean and fresh top surface of the HOPG sample was obtained [17]. A silicon dioxide (SiO₂) film was then grown on the sample top surface by plasma enhanced chemical vapor deposition (PECVD), and then followed by electron beam lithography and reaction ion etching. Figure 2(b) shows the scanning electron microscopy (SEM, FEI Quanta 200F) image of an obtained island with typical length 2-5 μ m and height 400nm. Figure 2(c) is the SEM image of the side-view of an island with the top flake tilted 30 degrees.

Similar to Ref. [15], we employed a micromanipulator MM3A (Kleindiek) that had been set in a SEM (FEI Quanta 200F) to perform our experiments under an ultrahigh vacuum condition (1.19 - 6.72×10^{-4} Pa) and the room temperature. Electron beam with 30 KV acceleration and 3 nm spot-size was used to monitor the fabrication process. The in situ process can be seen from Supplementary Movie. Schematically we show the experimental process in Fig. 3. We placed the MM3A tip on the top surface of a selected island and then pushed it in a lateral direction (Fig. 3(a)). A graphite/SiO₂ flake was then sheared out from its platform (base flake of the graphite island). The flake was found to be fully selfretractable after removing the tip. Our study on the self-retraction mechanism has revealed that the slipping plane corresponds to a boundary between two single-crystalline graphite grains and the original assembling between the moved flake and platform (before shear) is not AB-stacked, which leads to the large-scale superlubricity [15, 18] and consequently the self-retraction motion. To prevent the self-retraction, we used the tip to rotate the flake for a certain angle until the flake was suddenly locked up, which corresponds to an ABstack assembling as revealed in our recent study [18]. In the experiment, pushing the locked top flake again in the opposite lateral direction leads to the separation of the flake into two parts: the top and the middle flakes. The observed self-retraction between these two separated flakes (See Supplementary Movie) indicates once more a non AB-stack contact. To prevent the self-retraction, we rotated the top flake with respect to middle flake to another 'lock-up' state (Fig. 3(d)), and finally two flakes over the platform are both locked-up.

The optical microscope (OM, HiRox KH-3000) image of a typical locked-up example in our experiments is shown in Fig. 3(e), where the top flake (blue colored) spanned over the middle graphite flake. Fig 3(f) shows the height profile along the black line in Fig. 3(e), obtained by using an atomic force microscope (AFM). The measured step height or the middle flake thickness is $\Delta^* = 53.7 \pm 0.9$ nm. In comparison, the height drop along the top

flake surface was measured as $\Delta = 53.8\pm2.7$ nm, which is almost the same as the thickness of the middle flake. Such a good agreement confirms the good adhesion of the top flake with the middle flake and platform. This negligible difference could come from the surface roughness of the SiO₂ thin film. The good adhesion is also supported by colour image in Fig. 3(e), where the blue color is fully reproduced at both flat sides of the top flake.

Figure 4(a) shows the AFM measured height profiles along the lines in the insert for the sample prepared in SEM as explained before. The thickness of the top flake is measured as $h=325\pm1$ nm and the height of the step (i.e., the thickness of the middle flake) is $\Delta=30\pm3$ nm. By using MM3A micromanipulator to take the top flake off its platform and then stand the flake up, we measured the thickness of the SiO₂ film as 205±8 nm (Fig. 4(b)). Using the measured values $\Delta=30$ nm, $h_s=20$ 5nm, $h_g=120$ nm, and well-accepted elastic constants of SiO₂ and graphite in our finite element (FEM) model (see details in Supplementary Information), we obtained the deflection curve y(x,L) of the top surface of the model graphite/SiO₂ flake at different span length L. Finally, we can quite accurately determine the span length L of each AFM measured height profile by least square fitting it to the y(x,L) results obtained from our FEM analysis. The actual L in our experiments should correspond to the L value with the least fitting error. One example of such fitting is given in Fig. 4(c) with the fitted span lengths L=890 nm. The error bound of L is estimated smaller than 20nm.

It should be noted that expressing the elastic strain energy U in Eq. (1) by an analytic model is rather difficult due to the following two aspects. First, the bulk graphite has the highest elastic anisotropy [19]: the highest in-plane elastic modulus (e.g., ~ 1000 GPa) and very weak interlayer shear modulus (e.g., ~ 4.5 GPa). The shear deformation near the interface between SiO₂ film and graphite flake is expected to be significant and difficult to theoretically model. Second, the elastic deformation of the step (made up by the middle flake and the platform) is difficult to describe as well, although it turns out to be important. Finite element method (FEM) analyses were thus employed to calculate the strain energy U. The details of FEM model are included in Supplementary Information (SI). Figure 1(b) plots the calculated strain energies U(L) and Fig. 1(c) gives the approximations of BE through following central finite difference of Eq. (1):

$$2\gamma(L) \approx -\frac{U(L + \delta L) - U(L - \delta L)}{2b \times \delta L},\tag{2}$$

with $\delta L = 20$ nm. Finally, the binding energy is approximated as 0.27 ± 0.02 J/m², corresponding to determined length $L = 890 \pm 20$ nm (Fig. 1 (c)).

To test the reliability of the above-proposed method, we measured the second island sample with different size and shape. The measured binding energy is $0.30 \pm 0.025 \text{ J/m}^2$, which agrees pretty well with the first sample shown in Figure 4(a). Details are given in SI.

It is well known that chemisorption, physisorption, and insertion of gases inside graphite can drastically change the surface/interface properties [20]. The binding energy of graphite under vacuum was estimated about 100 times higher those in an environment with air, oxygen or water vapor [21]. To avoid such artificial effects, we note again that above-reported experiments are carried out in SEM with ultra-high vacuum condition. Similar experiments but in atmospheric conditions were also done using an MM3A assisted by an optical microscope. The binding energy measured is just a little smaller than that from SEM, $\sim 0.22 \text{J/m}^2$. We believe that the self-retraction motion of graphite/SiO₂ flakes can self-clean the adsorbate on the exposed sliding surfaces [22].

In summary, a novel experimental method is presented here to directly measure the interlayer binding energy of highly oriented pyrolytic graphite: $2\gamma = 0.27 \pm 0.02 \text{ J/m}^2$ (or $44 \pm 3 \text{ meV/atom}$). The error bar is mainly caused by the roughness of the top SiO₂ thin film. It can be improved significantly by either extracting a smoother deflection profile from comparison of the AFM height profiles along lines on top flakes before and after its spanning over the step, or simply using other types of top thin films and improved ion etching process. Our proposed method can be easily extended to measure the binding energies between the graphite/graphene and other types of substrates. It can also be used in other systems, particularly lamellar materials and thin films. Considering the difficulty in measuring the interface binding energy in micro/nano-materials, our method could serve as a general solution.

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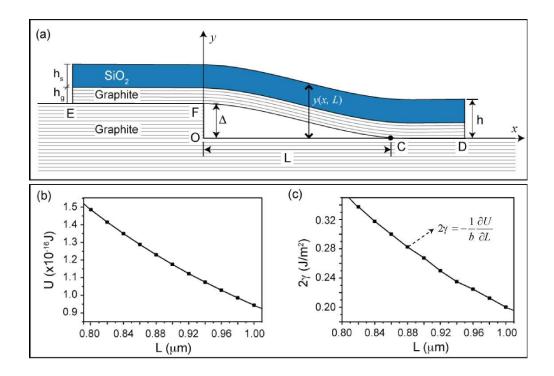


FIG. 1: (color online) (a) Sketch image of a graphite/SiO₂ flake spanned a graphite step of height Δ with spanned length L. (b) The system strain energy (black square dots) versus spanned length obtained by using ABAQUS simulations, where the width is set as a unit for plane strain and the other parameters ($\Delta = 30$ nm, $h_s = 205$ nm, $h_g = 120$ nm) are the measured values using AFM and SEM, see text for details. (c). The binding energy obtained by central finite difference of the data in (b)

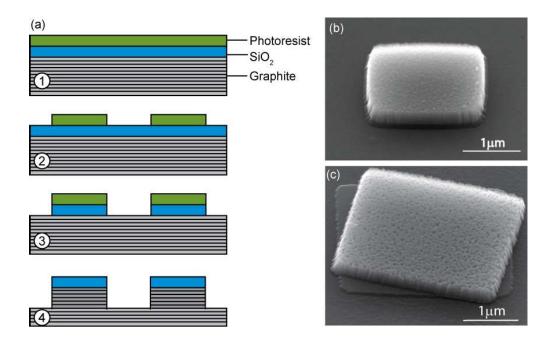


FIG. 2: (color online) (a) Fabrication illustration of the graphite islands. SiO₂ thin film is grown on top of the island by using plasma enhanced chemical vapor deposition. Electron beam lithography and reaction ion etching is then used to fabricate the island. (b)(c) Scanning electron microscopy image of the side-view of the fabricated island as the sample stage tilted 30 degrees.

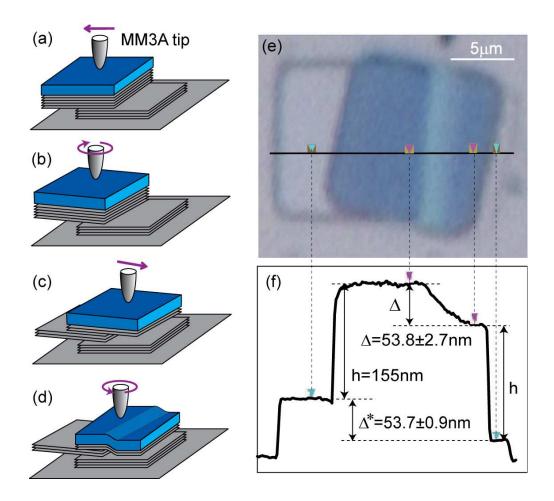


FIG. 3: (color online) Illustration of the experimental process. (a) An MM3A tip is used to slide a graphite/SiO₂ flake with respect to the bottom flake. (b) The graphite/SiO₂ flake is then rotated by a certain angle to a 'lock-up' state (See text and Supplementary Movie). (c) After that the tip is moving in the opposite direction to split the slided flake into two parts: top and middle flake. (d) The top flake is spanned over the middle and bottom flakes and then it is rotated by the MM3A tip to another 'lock-up' state. (e) The optical microscope image of one obtained sample. (f) The profile obtained by atomic force microscopy (AFM) indicates that the adhesion is indeed taken place. The blue color in (e) reveals the constructive interference of $\sim \lambda/2$ (130nm) thickness of SiO₂ layer, that is consistent with the measurement in (f) The appearance of a greenish blue band in (e) reveals that the slope surface is quite uniform in width direction.

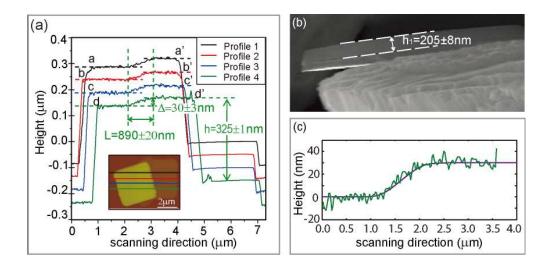


FIG. 4: (color online) AFM height profiles along the colored lines in Inset of a double locked-up sample prepared in a SEM in a high vacuum condition. These profiles are shifted for visulization clarity. (b) A graphite/SiO₂ flake adhered to a tip (bottom), showing the tickness of the SiO₂ film to be 205 ± 8 nm. (c) One representative least square fittings of deflection curves, yielding a consistent span length $L=890\pm20$ nm for each of the four profiles.